### PUBLICATION

# THE SECOND ORDER TRAFFIC FINE

Temporal reasoning in European Transport Regulations

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We argue that European transport regulations can be formalized within the purely existential fragment of monadic second-order logic and possibly weaker fragments including linear temporal logic. We consider several articles in the regulation to verify these claims.

## FORMALIZATION OF LEGAL ONTOLOGIES

Law Modelling of the EU Regulation: Regulation (EC) No 561/2006

#### Time

Modelling the regulation's articles via Linear Temporal Logic **Complexity** Expressibility of the legal articles within Monadic second-order Logic

## EXAMPLES



Illegal interval of six consecutive weeks performed by a hypothetical driver. (Fig. 2, p. 4)

	15	111	15	24	45 + 1

First five weeks of the example represented in Figure 2, together with a possible sixth week that would make the whole interval legal. (Fig. 3, p.4)



General example of arbitrary length of an illegal interval that is legal when week A or week B is erased. (Fig. 6, p. 5)

## CONCLUSIONS

Articles §8.6 or §8.9 cannot be expressed in the next-henceforth fragment (U-free fragment of LTL). §8.6 can only be expressed, if at all possible, in the full language of LTL (□-free fragment of LTL) with a large until-depth.

Both §8.6 and §8.9 can be expressed in a purely existential fragment of MSO (or monadic temporal logic). Evaluating whether a given truck driver's record complies with regulations can then be transformed into a model-checking problem over this fragment, and modelchecking formulas in this fragment can be reduced to satisfiability of first-order formulas.

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